

## Representations

- What you should know:
  - $\text{Base}^{(\# \text{ digits})} = \text{number of combinations}$
  - Examples:
    - Decimal:
      - 1 decimal digit = 10 combinations (0-9)
      - 2 decimal digits = 100 combinations (0-99)
      - Etc.
    - Binary
      - 1 binary digit = 2 combinations (0 to 1)
      - 2 binary digits = 4 combinations (00 to 11)
      - Etc.
    - $N^{\text{ary}}$  base e.g.  $n = 8$  (octal), 16 (hexadecimal) etc.
      - 1 digit =  $N$  combinations (0 to  $N-1$ )
      - 2 digits =  $N \times N$  combinations (0 to  $(N \times N)-1$ )
      - 3 digits =  $N \times N \times N$  combinations (0 to  $(N \times N \times N)-1$ )

James Tam

## Applying Precedence/Order Of Operation

- Name of the complete example: 1determiningOrder.py

James Tam

## 'Classic' Questions That Apply These Concepts

- Generic question:
  - Given you have 9 values to represent what is the minimum number of bits needed to store all n values.
- Tam question: The Borg<sup>1</sup> alphabet consists 66 symbols. How many bits would the Bynars<sup>1</sup> (0 to (N×N)-1) need to encode each letter?
- Try to work these out on your own (answer at the end of these notes).

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James Tam

## Applying Precedence/Order Of Operation

- How to evaluate a logical expression when bracketing is not used.<sup>1</sup>
- Example:

```
if True or False and not True:
    print("Expression true")
else:
    print("Expression false")
```

<sup>1</sup> JT's comment: you should always use brackets to make things clear but you may be required to trace the code of another person does not.

James Tam

## Applying Precedence/Order Of Operation

- How to evaluate a logical expression when bracketing is not used.
- Evaluating the Boolean expression:

True or False and not True

### Precedence rules

Order	Operations	Precedence
1	()	Highest
2	x ** y	
3	-x, +x	
4	x * y, x / y, x % y, x // y	
5	x + y, x - y	
6	<, <=, >, >=	
7	!=, ==	
8	not	
9	and	
10	or	
11	=	Lowest

James Tam

## Applying Precedence/Order Of Operation

- How to evaluate a logical expression when bracketing is not used.
- Evaluating the Boolean expression:

True or False and not True

Highest  
precedence

### Precedence rules

Order	Operations	Precedence
1	()	Highest
2	x ** y	
3	-x, +x	
4	x * y, x / y, x % y, x // y	
5	x + y, x - y	
6	<, <=, >, >=	
7	!=, ==	
8	not	
9	and	
10	or	
11	=	Lowest

James Tam

## Applying Precedence/Order Of Operation

- How to evaluate a logical expression when bracketing is not used.
- Evaluating the Boolean expression:
  - NOT has been evaluated

Next highest  
True or False and True



### Precedence rules

Order	Operations	Precedence
1	()	Highest
2	x ** y	
3	-x, +x	
4	x * y, x / y, x % y, x // y	
5	x + y, x - y	
6	<, <=, >, >=	
7	!=, ==	
8	not	
9	and	
10	or	
11	=	Lowest

James Tam

## Applying Precedence/Order Of Operation

- How to evaluate a logical expression when bracketing is not used.
- Evaluating the Boolean expression:
  - AND has been evaluated

Remaining operator  
True or False



### Precedence rules

Order	Operations	Precedence
1	()	Highest
2	x ** y	
3	-x, +x	
4	x * y, x / y, x % y, x // y	
5	x + y, x - y	
6	<, <=, >, >=	
7	!=, ==	
8	not	
9	and	
10	or	
11	=	Lowest

James Tam

## Applying Precedence/Order Of Operation

- How to evaluate a logical expression when bracketing is not used.
- Evaluating the Boolean expression:
  - OR has been evaluated
  - Final result of compound Boolean

```
if(True):  
    print("Expression true")
```

### Precedence rules

Order	Operations	Precedence
1	()	Highest
2	x ** y	
3	-x, +x	
4	x * y, x / y, x % y, x // y	
5	x + y, x - y	
6	<, <=, >, >=	
7	!=, ==	
8	not	
9	and	
10	or	
11	=	Lowest

James Tam

## Precedence/Order Of Operation: A More Complex Example

- Name of the complete example: 2determiningOrder.py

James Tam

## Applying Precedence/Order Of Operation

- How to evaluate a logical expression when bracketing is not used.
- Evaluating the Boolean expression in the branch.

First in a left-to-right order

if  $2 < 3$  or  $3 \neq 3$  and not  $2 < -2$ :

### Precedence rules

Order	Operations	Precedence
1	()	Highest
2	$x ** y$	
3	$-x$ , $+x$	
4	$x * y$ , $x / y$ , $x \% y$ , $x // y$	
5	$x + y$ , $x - y$	
6	$<$ , $<=$ , $>$ , $>=$	
7	$!=$ , $==$	
8	not	
9	and	
10	or	
11	$=$	Lowest

James Tam

## Applying Precedence/Order Of Operation

- How to evaluate a logical expression when bracketing is not used.
- Evaluating the Boolean expression in the branch.

Next highest ordering

if FALSE or  $3 \neq 3$  and not FALSE:

### Precedence rules

Order	Operations	Precedence
1	()	Highest
2	$x ** y$	
3	$-x$ , $+x$	
4	$x * y$ , $x / y$ , $x \% y$ , $x // y$	
5	$x + y$ , $x - y$	
6	$<$ , $<=$ , $>$ , $>=$	
7	$!=$ , $==$	
8	not	
9	and	
10	or	
11	$=$	Lowest

James Tam

## Applying Precedence/Order Of Operation

- How to evaluate a logical expression when bracketing is not used.
- Evaluating the Boolean expression in the branch.

### Precedence rules

Order	Operations	Precedence
1	()	Highest
2	x ** y	
3	-x, +x	
4	x * y, x / y, x % y, x // y	
5	x + y, x - y	
6	<, <=, >, >=	
7	!=, ==	
8	not	
9	and	
10	or	
11	=	Lowest

Next highest  
ordering

if FALSE or TRUE and not FALSE:

James Tam

## Applying Precedence/Order Of Operation

- How to evaluate a logical expression when bracketing is not used.
- Evaluating the Boolean expression in the branch.

### Precedence rules

Order	Operations	Precedence
1	()	Highest
2	x ** y	
3	-x, +x	
4	x * y, x / y, x % y, x // y	
5	x + y, x - y	
6	<, <=, >, >=	
7	!=, ==	
8	not	
9	and	
10	or	
11	=	Lowest

Next highest  
ordering

if FALSE or TRUE and TRUE:

James Tam

## Applying Precedence/Order Of Operation

- How to evaluate a logical expression when bracketing is not used.
- Evaluating the Boolean expression in the branch.

### Precedence rules

Order	Operations	Precedence
1	()	Highest
2	x ** y	
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4	x * y, x / y, x % y, x // y	
5	x + y, x - y	
6	<, <=, >, >=	
7	!=, ==	
8	not	
9	and	
10	or	
11	=	Lowest

Remaining  
operator  
if FALSE or TRUE:

James Tam

## Applying Precedence/Order Of Operation

- How to evaluate a logical expression when bracketing is not used.
- Evaluating the Boolean expression in the branch.

### Precedence rules

Order	Operations	Precedence
1	()	Highest
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6	<, <=, >, >=	
7	!=, ==	
8	not	
9	and	
10	or	
11	=	Lowest

Final result  
if TRUE:

The Tamman says again: "Bracket everything".  
You will sleep better and live a happier more fulfilling life (maybe not but you'll aggravate your programming team mates less).

James Tam



## Answer To The Questions Applying Representations

James Tam

### 'Classic' Questions That Apply These Concepts

- **Generic question:**

- Given you have 9 values to represent what is the minimum number of bits needed to store all n values.
- **Answer: 4 bits.** Using 3 bits is insufficient as not all values can be store with only 8 combinations. Although using 4 bits results in 7 used combinations this occurs in real life applications e.g. ASCII only requires 7 bits to encode the character information but 8 are used.

- **Tam question:** The Borg<sup>1</sup> alphabet consists 66 symbols. How many bits would the Bynars<sup>1</sup> (0 to (N×N)-1) need to encode each letter?

- **Answer: 7 bits.**

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James Tam