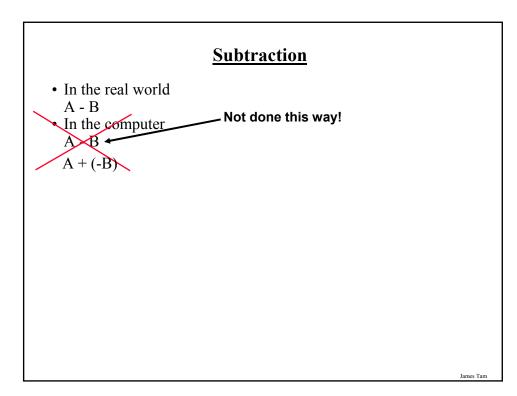


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Binary Subtraction Requires the complementing of a binary number i.e., A – B becomes A + (-B) The complementing can be performed by representing the negative number as a One's or Two's complement value.

James Tam

<u>Complementing Binary Using The Ones</u> <u>Complement Representation</u>

For positive values there is no difference (no change is needed)
e.g., positive seven (The 'A' in the expression A – B)

0111 (regular binary) 0111 (1's complement equivalent)

• For negative values complement the number by negating the

binary values: reversing (flipping) the bits (i.e., a 0 becomes 1 and 1 becomes 0).

e.g., minus six (The 'B' in the expression A – B becomes A+(-B))
 -0110 (regular binary)

1001 (1's complement equivalent)

<u>Complementing Binary Using The Twos</u> <u>Complement Representation</u>

• For positive values there is no difference (no change is needed)

e.g., positive seven (The 'A' in the expression A – B)
 0111 (regular binary)

0111 (2's complement equivalent)

• For negative values complement the number by negating the number: reversing (flipping) the bits (i.e., a 0 becomes 1 and 1 becomes 0) *and adding one to the result*.

e.g., minus six (The 'B' in the expression A – B becomes A+(-B))
 -0110 (regular binary)

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1010 (2's complement equivalent)

Representing Negative Numbers

•Real world

- Negative numbers – same as the case of positive numbers but precede the number with a negative sign "-" e.g., -123456.

•Computer world

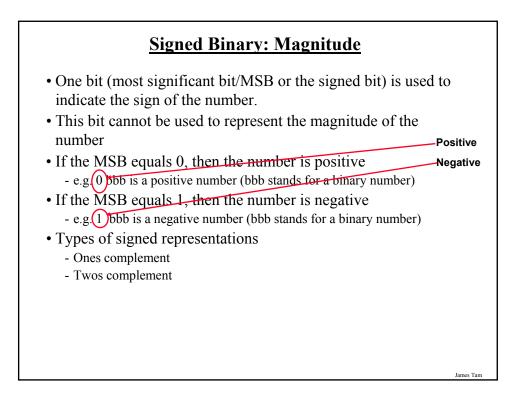
- Negative numbers - employ signed representations.

James Tam

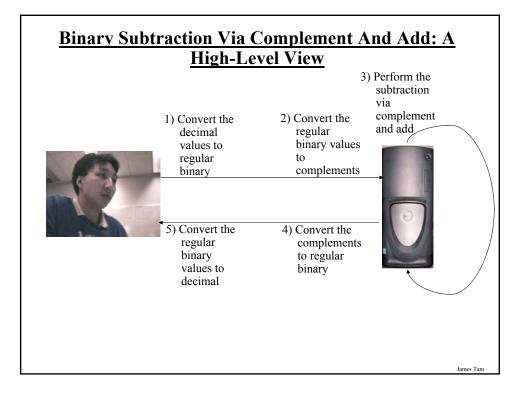
James Tan

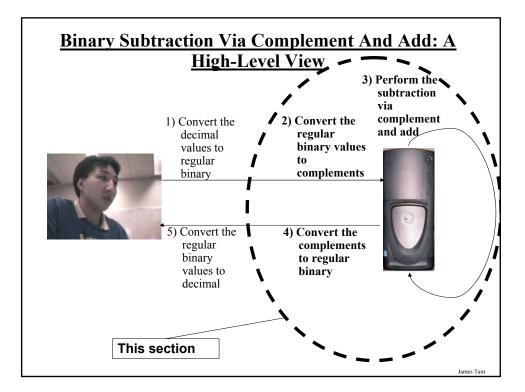
Signed Binary: Magnitude

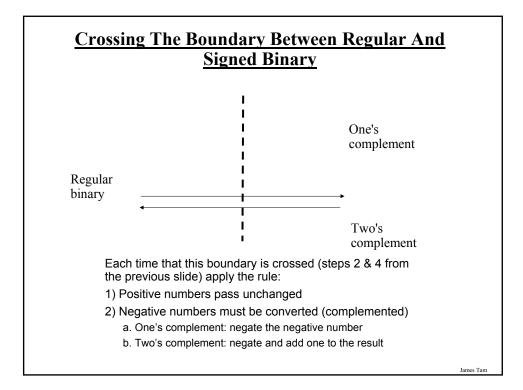
- One bit (most significant bit/MSB or the signed bit) is used to indicate the sign of the number.
- This bit cannot be used to represent the magnitude of the number
- If the MSB equals 0, then the number is positive - e.g. 0 bbb is a positive number (bbb stands for a binary number)
- If the MSB equals 1, then the number is negative - e.g. 1 bbb is a negative number (bbb stands for a binary number)
- Types of signed representations
 - Ones complement
 - Twos complement

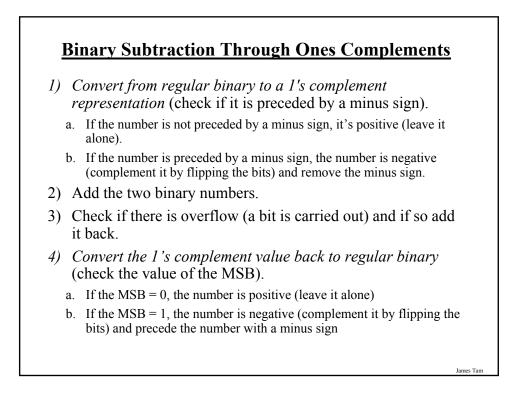


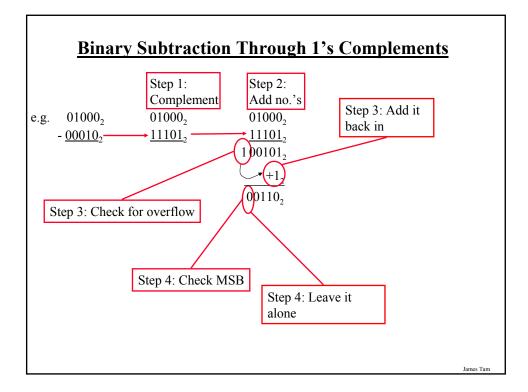
Bit pattern	Regular binary	Ones complement	Twos complement		
0000	0	0	0		
0001	1	1	1		
0010	2	2	2		
0011	3	3	3		
0100	4	4	4		
0101	5	5	5		
0110	6	6	6		
0111	7	7	7		
1000	8	-7	-8		
1001	9	-6	-7		
1010	10	-5	-6		
1011	11	-4	-5		
1100	12	-3	-4		
1101	13	-2	-3		
1110	14	-1	-2		
1111	15	-0	-1		











(with	s –around		ve enoug	h bits	to repres	sent a val	ue
Binary (1 bit)	Value	Binary (2 bits)	Value		Binary (3 bits)	Value	
0	0	00	0		000	0	
1	1	01	1		001	1	
0	0	10	2		010	2	
:	:	11	3		011	3	
		00	0		100	4	
		:	:		101	5	
					110	6	
					111	7	
					000	0	
					:		

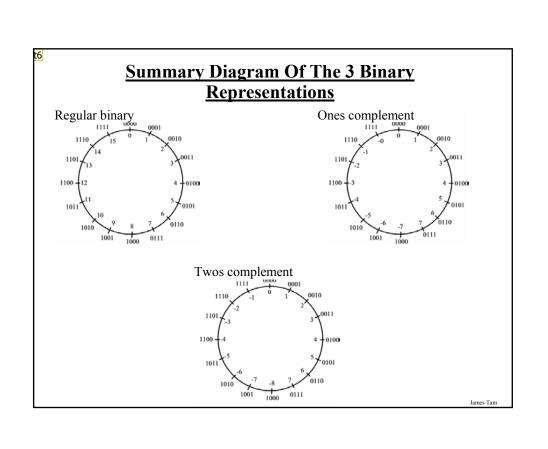
Overflow: Signed

- In all cases it occurs do to a "shortage of bits"
- Subtraction subtracting two negative numbers results in a positive number.

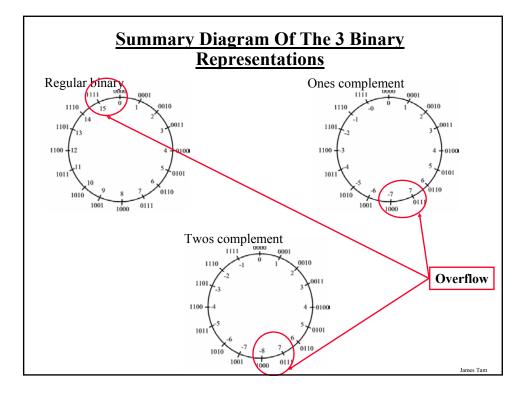
e.g. - 7 - <u>1</u> + 7

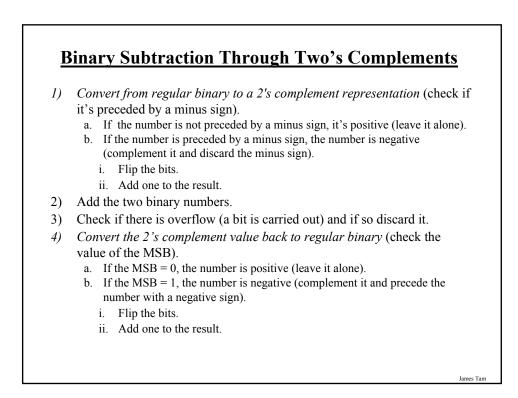
• Addition – adding two positive numbers results in a negative number.

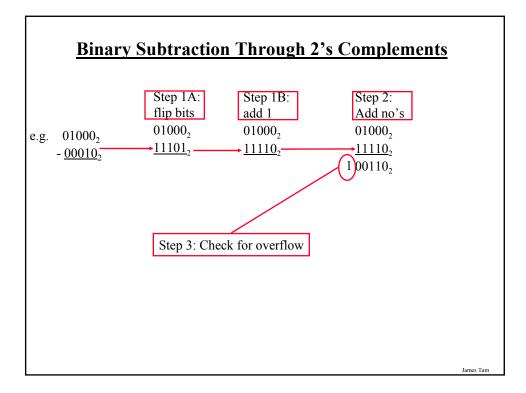
e.g. 7 + <u>1</u> - 8

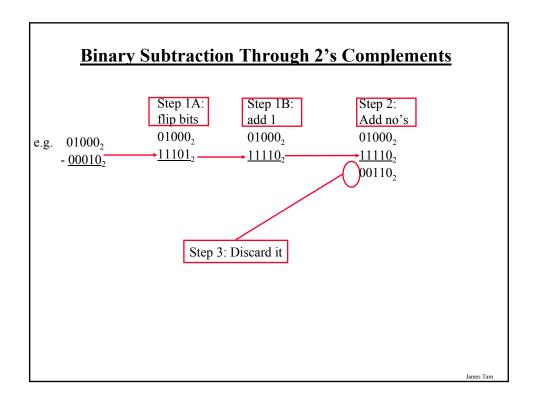


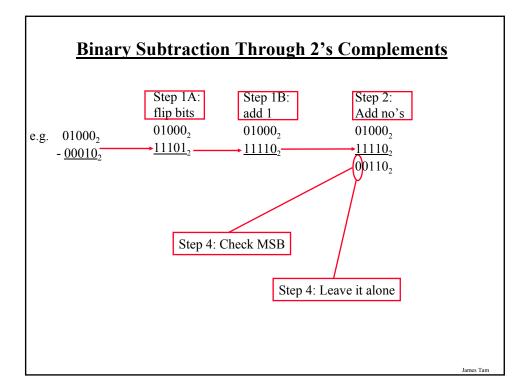
t6 Redo these three diagrams because they print funny tamj, 19/08/2005

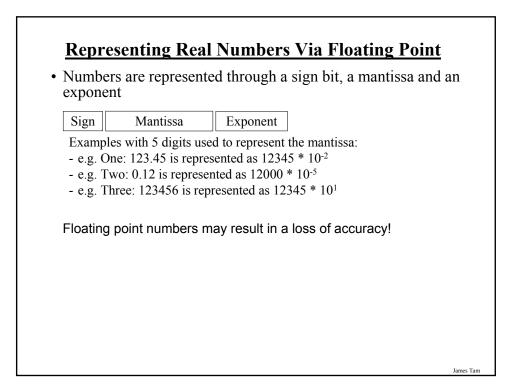












You Should Now Know

- •How negative numbers are represented using 1's and 2's complement representations.
- •How to convert regular binary to values into their 1's or 2's complement equivalent.
- •What is signed overflow and why does it occur.
- •How to perform binary subtractions via the negate and add technique.
- •How are real numbers represented through floating point representations

James Tam