



<u>Binary</u>

Base two

Employs two unique symbols (0 and 1)

Largest decimal value that can be represented by 1 binary digit = 1 = base(2) - 1

| Decimal value | Binary value | Decimal value | Binary value |
|---------------|--------------|---------------|--------------|
| 0 | 0000 | 8 | 1000 |
| 1 | 0001 | 9 | 1001 |
| 2 | 0010 | 10 | 1010 |
| 3 | 0011 | 11 | 1011 |
| 4 | 0100 | 12 | 1100 |
| 5 | 0101 | 13 | 1101 |
| 6 | 0110 | 14 | 1110 |
| 7 | 0111 | 15 | 1111 |

Why Bother With Binary?

Representing information

- ASCII (American Standard Code for Information Interchange)
- Unicode

It's the language of the computer

James Tam

Representing Information: ASCII

| Decimal | Binary | ASCII |
|-----------|---------------------|--|
| 0-31 | 00000000 - 00011111 | Invisible (control characters) |
| 32 - 47 | 00100000 - 00101111 | Punctuation, mathematical operations |
| 48 - 57 | 00110000 - 00111001 | Characters 0 - 9 |
| 58 - 64 | 00111010 - 01000000 | Comparators and other miscellaneous characters : ; ? @ |
| 65 - 90 | 01000001 - 01011010 | Alphabetic (upper case A - Z) |
| 91 – 96 | 01011011 - 01100000 | More miscellaneous characters [\]^_' |
| 97 – 122 | 01100001 - 01111010 | Alphabetic (lower case a - z) |
| 123 – 127 | 01111011 - 01111111 | More miscellaneous characters { } ~ DEL |

Representing Information: ASCII (2)

Uses 7 bits to represent characters

Max number of possibilities = $2^7 = 128$ characters that can be represented

e.g., 'A' is 65 in decimal or 01000001in binary. In memory it looks like this:



Representing Information: Unicode

Uses 16 bits (or more) to represent information

Max number of possibilities = $2^{16} = 65536$ characters that can be represented (more if more bits are used)





| Decimal value | Octal value | Decimal value | Octal value |
|---------------|-------------|---------------|-------------|
| 0 | 0 | 8 | 10 |
| 1 | 1 | 9 | 11 |
| 2 | 2 | 10 | 12 |
| 3 | 3 | 11 | 13 |
| 4 | 4 | 12 | 14 |
| 5 | 5 | 13 | 15 |
| 6 | 6 | 14 | 16 |
| 7 | 7 | 15 | 17 |



| Machine | Octal | PDP -11 assembly |
|---------------|--------|------------------|
| language | value | language |
| 1010111000000 | 012700 | MOV #4, R0 |
| 1001010000101 | 011205 | MOV (R2), R5 |

from Introduction to the PDP-11 and its Assembly Language by Frank T

Hexadecimal (Hex)

Base sixteen

Employs sixteen unique symbols (0 - 9, followed by A - F)

Largest decimal value that can be represented by 1 hex digit = 15

| Decimal value | Hexadecimal value | Decimal value | Hexadecimal value |
|---------------|-------------------|---------------|-------------------|
| 0 | 0 | 9 | 9 |
| 1 | 1 | 10 | A |
| 2 | 2 | 11 | В |
| 3 | 3 | 12 | C |
| 4 | 4 | 13 | D |
| 5 | 5 | 14 | E |
| 6 | 6 | 15 | F |
| 7 | 7 | 16 | 10 |
| 8 | 8 | 17 | 11 |

Uses Of Hexadecimal (Assembly Language)

| Machine | Hexadecimal | 680X0 assembly | |
|-----------------|-------------|-----------------|--|
| language | value | language | |
| 1010011000001 | 14C1 | MOV.B D1, (A2)+ | |
| 110000011100000 | 60E0 | BRA NEXT | |
| | | | |
| | | | |
| | | | |
| | | | |
| | | | |
| | | | |
| | | | |

| Decimal | Binary | Octal | Hex | Decimal | Binary | Octal | Hex |
|---------|--------|-------|-----|---|--------|-------|-----|
| 0 | 0000 | 0 | 0 | 8 | 1000 | 10 | 8 |
| 1 | 0001 | 1 | 1 | 9 | 1001 | 11 | 9 |
| 2 | 0010 | 2 | 2 | 10 | 1010 | 12 | A |
| 3 | 0011 | 3 | 3 | 11 | 1011 | 13 | В |
| 4 | 0100 | 4 | 4 | 12 | 1100 | 14 | C |
| 5 | 0101 | 5 | 5 | 13 | 1101 | 15 | D |
| 6 | 0110 | 6 | 6 | 14 | 1110 | 16 | E |
| 7 | 0111 | 7 | 7 | 15 ¹¹¹¹¹¹¹¹¹¹¹¹¹¹¹¹¹¹¹¹¹¹¹¹¹¹¹¹¹¹¹¹¹¹¹ | 1111 | 17 | F |





| | | , 2010) | | | | |
|-------------------|-------|--------------------|-------|--------------------|-------|--|
| Binary (1 bit) | Value | Binary (2 bits) | Value | Binary (3 bits) | Value | |
| 0 | 0 | 00 | 0 | 000 | 0 | |
| 1 | 1 | 01 | 1 | 001 | 1 | |
| 0 | 0 | 10 | 2 | 010 | 2 | |
| 1 | 1 | 11 | 3 | 011 | 3 | |
| - | | 00 | 0 | 100 | 4 | |
| | | 01 | 1 | 101 | 5 | |
| | | 01 | 1 | 110 | 6 | |
| | | 10 | 2 | 111 | 7 | |
| | | 11 | 3 | 000 | 0 | |
| | | | | 001 | 1 | |
| | | • | • | 001 | 1 | |
| | | | | : | : | |

Arbitrary Number Bases

Base N

Employs N unique symbols

Largest decimal value that can be represented by 1 digit = Base (N) - 1

Converting Between Different Number Systems

Binary to/from octal

Binary to/from hexadecimal

Octal to/from hexadecimal

Decimal to any base

Any base to decimal

James Tam

Binary To Octal

3 binary digits equals one octal digit (remember 2³=8)

Form groups of three starting at the decimal

•For the integer portion start grouping at the decimal and go left

•For the fractional portion start grouping at the decimal and go right

Octal To Binary

1 octal digit equals = 3 binary digits

Split into groups of three starting at the decimal

•For the integer portion start splitting at the decimal and go left

•For the fractional portion start splitting at the decimal and go right



Binary To Hexadecimal

4 binary digits equals one hexadecimal digit (remember $2^4=16$)

Form groups of four at the decimal

•For the integer portion start grouping at the decimal and go left

•For the fractional portion start grouping at the decimal and go right

e.g.,
$$1000.0100_2 = ???_{16}$$

8 . 4₁₆

Hexadecimal To Binary

1 hex digit equals = 4 binary digits

Split into groups of four starting at the decimal

•For the integer portion start splitting at the decimal and go left

•For the fractional portion start splitting at the decimal and go right











Decimal To Any Base

- 1) Split up the integer and the fractional portions
- 2) For the integer portion, keep dividing by the target base until the quotient is less than the target base
- 3) For the fractional portion, keep multiplying by the target base until either the resulting product equals zero (or you have the desired number of places of precision)













You Should Now Know

•What is meant by a number base

- •How binary, octal and hex based number systems work and what role they play in the computer
- •What is overflow, why does it occur and when does it occur
- •How to convert between non-decimal based number systems and decimal
- •How to perform simple binary math (addition and subtraction)