## CPSC 351 — Tutorial Exercise #15 Additional Practice Problem

This problem will not be discussed during the tutorial, and solutions for this problem will not be made available. It can be used as a "practice" problem that can help you practice skills considered in the lecture presentation for Lectures #15–17, or in Tutorial Exercise #15.

1. Consider the following decision problem:

## The Language Subset Problem

*Instance:* A pair of Turing machines,  $M_1$  and  $M_2$ , with the same input alphabet *Question:* Is  $L(M_1)$  a subset of  $L(M_2)$ ?

Suppose that instances of this problem are encoded as strings over an alphabet  $\Sigma_{2TM}$  as described in the lecture presentation for Lecture #17, so that  $Pair_{TM}$  is the language of instances of this decision problem (just as it was for the decision problem considered in that lecture presentation). Let  $Subset_{TM} \subseteq Pair_{TM}$  be the language of Yes-instances of this decision problem.

Prove that the Language Subset Problem is undecidable. That is, prove that the language Subset $_{\mathsf{TM}}$  is undecidable.