## CPSC 351 — Tutorial Exercise #15 Many-One Reductions II

These questions are intended to give you practice in establishing *many-one reductions* between languages. They are of the difficulty, and length, that would be appropriate for a question on an *assignment* in CPSC 351.

## **Problem To Be Solved**

1. Consider the following decision problem.

## The Rejection Problem

Instance: A Turing machine

$$M = (Q, \Sigma, \Gamma, \delta, q_0, q_{\text{accept}}, q_{\text{reject}})$$

and an input string  $\omega \in \Sigma^*$  for M.

Question: Does M reject M?

Let us use the same alphabet  $\Sigma_{\mathsf{TM}}$  and encoding for Turing machines and input strings as in Lecture #13, so that the language decidable language  $L_{\mathsf{TM+l}} \subseteq \Sigma_{\mathsf{TM}}^{\star}$ , introduced in that lectures, is the *language of instances* of this decision problem. Let Reject\_{\mathsf{TM}} \subseteq L\_{\mathsf{TM+l}} be the *language of Yes-instances* of this decision problem.

Prove that the Rejection Problem is undecidable — that is, prove that the above language,  $Reject_{TM}$ , is undecidable.

A *hint* for this problem is available in a separate file — but you should spend at least a little bit of time trying to solve this problem, without looking at it, before you use this hint.