

Lecture #21: Tail Bounds

Questions for Review

1. What is **Markov's Inequality**?
2. What is the **variance** of a random variable (with respect to a probability distribution P)? Please give a second (equivalent) formula for the variance that is often used as well.
3. What is the **standard deviation** of a random variable X (with respect to a probability distribution P)?
4. Suppose now that n is an integer such that $n \geq 2$ and

$$X = X_1 + X_2 + \cdots + X_n.$$

Describe a property of the random variables X_1, X_2, \dots, X_n (which, unfortunately, does not always hold) that makes it reasonably easy to compute the variance of X from the variances of X_1, X_2, \dots, X_n .

5. What is **Chebyshev's Inequality**?
6. What is **Cantelli's Inequality**? What other name(s) does this bound have?
7. What is the **Chernoff Bound**? This cannot always be applied when some, or all, of the rest of the results (used to bound probabilities), given in this lecture, can. When *can* it be applied?
8. Quite a few of the results, described in the preparatory reading material, depend on an **assumption** about the sample space, Ω . What is this assumption?