

# Lecture #13: First Undecidable and Unrecognizable Languages

## Questions for Review

1. Describe the languages  $TM$  and  $TM+1$ . Are they recognizable? Are they decidable?
2. Describe the language  $A_{TM}$ . Is this language recognizable? Is this decidable?
3. OK, OK... the language  $A_{TM}$  was proved to be **undecidable** in Lecture #13 — and this the first language proved to undecidable, so far, in this course.  
What **proof technique** was used to prove this?
4. Now consider the **complement**  $A_{TM}^C$  of  $A_{TM}$ . Is *this* language decidable? Is it recognizable?
5. OK, OK... the language  $A_{TM}^C$  was proved to be **unrecognizable** in Lecture #13 — and this is the first language proved to be unrecognizable, in this course.  
What **proof technique** was used to prove this?